# Package: polyMatrix (via r-universe)

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**Version** 0.9.11

**Title** Infrastructure for Manipulation Polynomial Matrices

**Description** Implementation of class ``polyMatrix" for storing a matrix of polynomials and implements basic matrix operations; including a determinant and characteristic polynomial. It is based on the package 'polynom' and uses a lot of its methods to implement matrix operations. This package includes 3 methods of triangularization of polynomial matrices: Extended Euclidean algorithm which is most classical but numerically unstable; Sylvester algorithm based on LQ decomposition; Interpolation algorithm is based on LQ decomposition and Newton interpolation. Both methods are described in D. Henrion & M. Sebek, Reliable numerical methods for polynomial matrix triangularization, IEEE Transactions on Automatic Control (Volume 44, Issue 3, Mar 1999, Pages 497-508) <doi:10.1109/9.751344> and in Salah Labhalla, Henri Lombardi & Roger Marlin, Algorithmes de calcule de la reduction de Hermite d'une matrice a coefficients polynomeaux, Theoretical Computer Science (Volume 161, Issue 1-2, July 1996, Pages 69-92) <doi:10.1016/0304-3975(95)00090-9>.

Type Package

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URL https://github.com/namezys/polymatrix

BugReports https://github.com/namezys/polymatrix/issues

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# RemoteRef HEAD

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# Description

The adjugate or classical adjoint of a square matrix is the transpose of its cofactor matrix. It is also occasionally known as adjunct matrix,[ though this nomenclature appears to have decreased in usage.

cbind 3

# Usage

```
adjoint(x)
## S4 method for signature 'polyMatrix'
adjoint(x)
```

# Arguments

x an matrix

### Methods (by class)

• polyMatrix: adjugate of polynomial matrix

cbind

Combine polynial matrices by rows or coluns

### **Description**

Combine polynial matrices by rows or coluns

# Usage

```
cbind(..., deparse.level = 1)
rbind(..., deparse.level = 1)
```

### **Arguments**

```
... (generalzed) vectors or mmatrices. If any of objects are polynomail matrix departs e.level details in base function, polynomial matrices doesn't use it
```

# Value

if at least one argument is a polynomail matrix, the result will be combined polynomial matrix. Overwise, base package implementatioon base::cbind() or base::rbind() will be called.

### **Functions**

• rbind: row based bind

# See Also

base::cbind()

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charpolynom

Characteristic polynomial of matrix

### **Description**

Characteristic polynomial of matrix

### Usage

```
charpolynom(x)

## S4 method for signature 'matrix'
charpolynom(x)

## S4 method for signature 'polynomial'
charpolynom(x)

## S4 method for signature 'polyMatrix'
charpolynom(x)

## S4 method for signature 'polyMatrixCharPolynomial,ANY'
x[[i]]

## S4 method for signature 'polyMatrixCharPolynomial'
degree(x)

## S4 method for signature 'polyMatrixCharPolynomial'
predict(object, newdata)

## S4 method for signature 'polyMatrixCharPolynomial'
show(object)
```

### **Arguments**

x an matrix

i the degree to extract polinomial coefficient

object an R object

newdata the value to evaluate

### **Details**

The characteristic polynom of a polynomial matrix is a polynom with polynomial coefficients.

# Value

When the input is a numerical matrix of matrix class then the value is a polynomial object. When the input is a polyMatrix object then a value is polyMatrixCharClass class object,

cofactor 5

### Methods (by class)

- matrix: for numerical matrix it is a polynomial with numerical coefficients
- polynomial: for polynomial it treats as a matrix 1x1
- polyMatrix: for polynomial matrix it has polynomial coefficients
- x = polyMatrixCharPolynomial, i = ANY: get polynomial coefficient of characteristic
- polyMatrixCharPolynomial: the degree of char polynomial of polynomial matrix
- polyMatrixCharPolynomial: value of char polynomial in polynomial point
- polyMatrixCharPolynomial: prints out a text representation of a characteristic polinomial of polinomial matrix

### See Also

```
polyMatrixCharClass
```

### **Examples**

cofactor

Cofactor of matrix

# Description

Cofactor of matrix

### Usage

```
cofactor(x, r, c)
```

### **Arguments**

```
x an matrix
```

r, c the row and column

### Value

cofactor which is number or polynomial

#### See Also

```
adjoint()
```

6 degree

degree

Gets maximum degree of polynomial objects

# Description

Returns the maximum degree as an integer number.

### Usage

```
degree(x)
## S4 method for signature 'numeric'
degree(x)
## S4 method for signature 'matrix'
degree(x)
## S4 method for signature 'polynomial'
degree(x)
## S4 method for signature 'polyMatrix'
degree(x)
```

### **Arguments**

Χ

an R objects

#### **Details**

By default, this function raises error for unknown type of object.

A numerical scalar has zero degree.

A numerical matrix has zero degree as each of its items has zero degree as well.

For polynomials this function returns the highest degree of its terms with non-zero coefficient.

### Value

The value is an integer number which can be different from zero only for polynomial objects.

# Methods (by class)

- numeric: a scalar argument always has zero degree
- matrix: a numerical matrix always has zero degree
- polynomial: the degree of a polynomial
- polyMatrix: the degree of a polynomial matrix is the highest degree of its elements

diag 7

# **Examples**

```
# numerical
degree(1) ## 0

# numerical matrix
degree(matrix(1:6, 3, 2)) ## 0

# polinomial
degree(parse.polynomial("1")) ## 0
degree(parse.polynomial("1 + x")) ## 1
degree(parse.polynomial("1 + x^3")) ## 3

# polynomial matrices
degree(parse.polyMatrix(
    "x; x^2 + 1",
    "0; 2x"))
## 2
```

diag

Polynomial matrix Diagonals Extract or construct a diagonal polynomial matrix.

# Description

Polynomial matrix Diagonals Extract or construct a diagonal polynomial matrix.

# Usage

```
diag(x = 1, nrow, ncol, names = TRUE)
## S4 method for signature 'polynomial'
diag(x, nrow, ncol)
## S4 method for signature 'polyMatrix'
diag(x)
```

### **Arguments**

x a polynomial matrix, or a polynomial, or an R objectnrow, ncol optional dimensions for the result when x is not a matrix.names not usedd

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### **Details**

In case of polynomail objets, diag has 2 distinct usage:

• x is a polynomial, it returns a polynomial matrix the given diagonal and zero off-diagonal entries.

• x is a polynomial matrix, it returns a vector as a polynomial matrix of diagonal elements

For polynomial, either nrow or ncol must be provided.

# Methods (by class)

- polynomial: for a polynomial, returns polynomial matrix with given diagonal
- polyMatrix: for a polynomial matrix extract diagonal For polynomial matrix, neither nrow and ncol can't be provided.

#### See Also

Base base::diag() for numericals and numerical matrices

### **Examples**

GCD 9

GCD

GCD for polynomial matrices

### **Description**

The greatest common divisor of polynomials or polynomial matrices.

# Usage

```
GCD(...)
## S4 method for signature 'polyMatrix'
GCD(...)
```

### **Arguments**

an list of polynomial objects

# Methods (by class)

• polyMatrix: the greatest common divisor of all elements of the polynomial matrice

### See Also

```
polynomial implementation polynom::GCD() and LCM()
```

### **Examples**

inv

Inverse polynomial matrix

### **Description**

During inversion we will try to round to zero

# Usage

```
inv(x, eps = ZERO\_EPS)
```

is.proper

# **Arguments**

x an polynomial matrix

eps zero threshold

### **Details**

Right now only matrices with numerical determinant is supported

is.polyMatrix

Check if object is polyMatrix

# **Description**

Check if object is polyMatrix

# Usage

```
is.polyMatrix(x)
```

### **Arguments**

Χ

an R object

### Value

TRUE if object is a polonial matrix

### **Examples**

```
is.polyMatrix(c(1, 2, 3))
is.polyMatrix(polyMatrix(0, 2, 2))
```

is.proper

Proper polynomial matrices

# Description

Tests the proper property of polynomial matrix. A polynomial matrix is proper if the associeted matrix has a full rank.

is.zero 11

### Usage

```
is.proper(pm)
is.column.proper(pm)
is.row.proper(pm)
```

### **Arguments**

pm

a polyMatrix objects

### **Details**

Polynomial matrix is column (row, full) proper (or reduced) if associated matrix has same rank as the number of column (row)

### Value

True if object pm is a (row-/column-) proper matrix

#### **Functions**

- is.column.proper: tests if its argument is a column-proper matrix
- is.row.proper: tests if its argument is a row-proper matrix

### **Examples**

is.zero

Test if something is zero

# **Description**

Generic function to check if we can treat on object as being zero. For matrices the result is a matrix of the same size.

is.zero

### Usage

```
is.zero(x, eps = ZERO_EPS)

## S4 method for signature 'polynomial'
is.zero(x, eps = ZERO_EPS)

## S4 method for signature 'polyMatrix'
is.zero(x, eps = ZERO_EPS)
```

### Arguments

x The checked object

eps Minimal numerical value which will not treat as zero

#### Details

Different type of objects can be treated as a zero in different ways:

- Numerical types can be compare by absolute value with eps.
- Customer types should define an an customer method.

By befault eps:

```
ZERO_EPS ## [1] 1e-05
```

#### Value

TRUE if the object can be treat as zero

### Methods (by class)

- polynomial: a polynomail can be treated as zero if all its coefficients can be treated as zero
- polyMatrix: for a polunomial matrix every item is checked as polynomial

### See Also

```
zero.round()
```

### **Examples**

```
# numericals and matrices
is.zero(0) ## TRUE
is.zero(0.0001, eps=0.01) ## TRUE
is.zero(c(0, 1, 0)) ## TRUE, FALSE, TRUE
is.zero(matrix(c(1, 9, 0, 0), 2, 2))
# FALSE TRUE
# FALSE TRUE
```

LCM 13

```
# polynomials is.zero(parse.polynomial("0.1 - 0.5 x")) ## FALSE is.zero(parse.polynomial("0.0001 - 0.0005 x + 0.00002 x^2"), eps=0.01) ## TRUE
```

LCM

LCM for polynomial matrices

# Description

The least common multiple of polynomials or polynomial matrices.

# Usage

```
LCM(...)
## S4 method for signature 'polyMatrix'
LCM(...)
```

### **Arguments**

... an list of polynomial objects

### Methods (by class)

• polyMatrix: the least common multiple of polynomial matrices

### See Also

```
polynomial implementation polynom::GCD() and GCD()
```

### **Examples**

```
# LCM of polynomial matrix
LCM(parse.polyMatrix(
   " 1 - x, 1 - x^2, 1 + 2*x + x^2",
   "x - x^2, 1 + x, 1 - 2*x + x^2"
)) ## 0.25*x - 0.5*x^3 + 0.25*x^5
```

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matrix.degree

Degree of each item of matrix

### **Description**

Returns a matrix obtained by applying a function degree() for each element of the matrix.

### Usage

```
matrix.degree(x)
## S4 method for signature 'matrix'
matrix.degree(x)
## S4 method for signature 'polynomial'
matrix.degree(x)
## S4 method for signature 'polyMatrix'
matrix.degree(x)
```

### **Arguments**

Х

an R object

# Details

Degree of each item is calculated using degree() which is defined for polynomials as the highest degree of the terms with non-zero coefficient.

For convenience this function is defined for any object, but returns zero for non polynomial objects.

#### Value

If the argument is a matrix, the result is a matrix of the same size containing the degrees of the matrix items.

For a numerical matrix the value is always a zero matrix of the same size

For a polynomial the value is the degree of the polynomial

### Methods (by class)

- matrix: the degree of a numerical matrix is a zero matrix for compatibility
- polynomial: the degree of a polynomial
- polyMatrix: a matrix of degrees for each polynomial item of the source matrix

minor 15

### **Examples**

```
# numerical matrices
matrix.degree(matrix(1:6, 2, 3))
        [,1] [,2] [,3]
           0
                0
## [1,]
## [2,]
                     0
           0
                0
# polynomials
matrix.degree(parse.polynomial("x + 1")) ## 1
matrix.degree(parse.polynomial("x^3 + 1")) ## 3
matrix.degree(parse.polynomial("1")) ## 0
# polynomial matrices
matrix.degree(parse.polyMatrix(
   "x; x^2 + 1",
   "0; 2x"))
       [,1] [,2]
## [1,]
         1
## [2,]
           0
```

minor

Minor of matrix item

# Description

A minor of a matrix A is the determinant of some smaller square matrix, cut down from A by removing one or more of its rows and columns. Minors obtained by removing just one row and one column from square matrices (first minors).

### Usage

```
minor(x, r, c)
```

# **Arguments**

x a matrix r, c row and column

newton

Build matrix of polynimal decomposition using Newton interpolation in Newton bais:  $(x-x_0)$ ,  $(x-x_0)$  \* $(xx_1)$ 

### **Description**

Build matrix of polynimal decomposition using Newton interpolation in Newton bais:  $(x-x_0)$ ,  $(x-x_0)$  \*  $(x x_1)$ 

parse.polyMatrix

### Usage

```
newton(C, points)
```

### **Arguments**

C Matrix of values of polinomials in columns

points point in which the values of polynomials were got

#### Value

Matrix of coefficients in columns (from higher degree to lower)

parse.polyMatrix

Parse polynomial matrix from strings

# Description

This is a convenient way to input a polynomial matrix.

### Usage

```
parse.polyMatrix(..., var = "x")
```

# **Arguments**

... string or strings to parse

var variable character. Only lower latin characters are allowed except 'e' which is

reseved for numbers

### **Details**

Space and tabulation characters are ignored.

Row should be divided by new line "\n" or backslash "\" (TeX style).

Elements in each row can be divided by ",", "; " or "&" (TeX style)

For convenience, this function can accept multiple string. In this case each string will be treated as a new row.

This function accepts TeX matrix format.

#### Value

new polynomial matrix of polyMatrix class

parse.polynomial 17

### **Examples**

parse.polynomial

Parse polynomial from string

# Description

Parse string representation of polynomial into a polynomial object.

### Usage

```
parse.polynomial(s, var = "x")
```

### **Arguments**

s an string for parsing var an variable name

### Value

new polynomial as polynom::polynomial object

polyMatrix

Create polyMatrix object

### **Description**

This function will create polynomial object fromm coefficient matrix or signle value

# Usage

```
polyMatrix(data, nrow, ncol, degree)
```

# **Arguments**

data	an matrix in case of creation from coefficient matrices or an numer/polynomial
nrow	A numer of rows of matrix. If data is a matrix, default value is the number of rows of data matrix. In other case, it's a required parameter
ncol	Must be positibe. If data is a matrix, default value is the number of columns of data matrix. In other ccase, it's a required parameter.
degree	Degree of polynomials in coefficient matrix. Can't be negative. If data is polynomial, degree can be evaluated automatcal. In other case, default value is 0.

### **Details**

A coefficient matrix is a matrix which contains matrices of coefficients from lower degree to higher side-by-side

### Value

new polynomial matrix of polyMatrix class

polyMatrix-class A class to represent matrix of polinomials

# **Description**

A class to represent matrix of polinomials

### Usage

```
## S4 method for signature 'polyMatrix,numeric'
x[[i]]

## S4 method for signature 'polyMatrix'
det(x)

## S4 method for signature 'polyMatrix'
nrow(x)

## S4 method for signature 'polynomial'
nrow(x)

## S4 method for signature 'polyMatrix'
ncol(x)

## S4 method for signature 'polyMatrix'
## S4 method for signature 'polyMatrix'
```

```
dim(x)
## S4 method for signature 'polyMatrix'
predict(object, newdata)
## S4 method for signature 'polyMatrix'
round(x, digits = 0)
## S4 method for signature 'polyMatrix'
show(object)
## S4 method for signature 'polyMatrix,missing,missing,missing'
x[i, j, ..., drop = TRUE]
## S4 method for signature 'polyMatrix,missing,ANY,missing'
x[i, j]
## S4 method for signature 'polyMatrix, ANY, missing, missing'
x[i, j]
## S4 method for signature 'polyMatrix,logical,logical,missing'
x[i, j]
## S4 method for signature 'polyMatrix,logical,numeric,missing'
x[i, j]
## S4 method for signature 'polyMatrix, numeric, logical, missing'
x[i, j]
## S4 method for signature 'polyMatrix,numeric,numeric,missing'
x[i, j]
## S4 replacement method for signature 'polyMatrix,missing,missing,ANY'
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix,missing,ANY,ANY'
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix, ANY, missing, ANY'
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix,numeric,numeric,numeric'
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix,numeric,numeric,matrix'
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix,numeric,numeric,polynomial'
```

```
x[i, j] \leftarrow value
## S4 replacement method for signature 'polyMatrix,numeric,numeric,polyMatrix'
x[i, j] \leftarrow value
## S4 method for signature 'polyMatrix,missing'
e1 + e2
## S4 method for signature 'polyMatrix,polyMatrix'
e1 + e2
## S4 method for signature 'polyMatrix,polynomial'
## S4 method for signature 'polyMatrix,numeric'
## S4 method for signature 'polyMatrix,matrix'
e1 + e2
## S4 method for signature 'ANY,polyMatrix'
e1 + e2
## S4 method for signature 'polyMatrix,polyMatrix'
e1 == e2
## S4 method for signature 'polyMatrix,polynomial'
e1 == e2
## S4 method for signature 'polyMatrix, matrix'
e1 == e2
## S4 method for signature 'polyMatrix,numeric'
e1 == e2
## S4 method for signature 'ANY,polyMatrix'
## S4 method for signature 'polyMatrix, ANY'
e1 != e2
## S4 method for signature 'ANY,polyMatrix'
e1 != e2
## S4 method for signature 'polyMatrix,polyMatrix'
x %*% y
## S4 method for signature 'polyMatrix, matrix'
```

```
x %*% y

## S4 method for signature 'matrix,polyMatrix'
x %*% y

## S4 method for signature 'polyMatrix,numeric'
e1 * e2

## S4 method for signature 'polyMatrix,polynomial'
e1 * e2

## S4 method for signature 'polyMatrix,polyMatrix'
e1 * e2

## S4 method for signature 'ANY,polyMatrix'
e1 * e2

## S4 method for signature 'polyMatrix,polyMatrix'
e1 - e2

## S4 method for signature 'polyMatrix,ANY'
e1 - e2

## S4 method for signature 'polyMatrix,ANY'
e1 - e2
```

### Arguments

x	an matrix object
i	the degree to extract matrix of coefficient
object	an R object
newdata	the value to evaluate
_	integer indicating the number of decimal places (round) or significant digits (signif) to be used
j	column indeces
•••	unused
drop	unused
value	new value
e1	an left operand
e2	an right operand
V	second argument

# Methods (by generic)

• [[: get coefficient matrix by degree

- det: determinant of a polynomial matrix
- nrow: number of rows of a polynomial matrix
- nrow: an polynomial has only one row
- ncol: number of column of a polynomial matrix
- ncol: an polynomial has only one column
- dim: dimension of a polynomial matrix
- predict: value of polynomial matrix in point
- round: round of polynomial matrix is rounding of polynomial coefficients
- show: prints out a text representation of a polynomial matrix
- [: get matrix content
- [: get columns
- [: get rows
- [: get by logical index
- [: get by logical index and numerical indeces
- [: get by logical index and numerical indeces
- [: get by row and column indeces
- [<-: replace matrix content
- [<-: assign rows
- [<-: assign columns
- [<-: assign part of matrix with number
- [<-: assign part of matrix with another matrix
- [<-: assign part of matrix with polynomial
- [<-: assign part of matrix with another polynomial matrix
- +: summation with polynomial matrix
- +: summation of polynomial matrices
- +: summation of polynomial matrix and scalar polynomial
- +: summation of polynomial matrix and scalar nummber
- +: summation of polynomial matrix and numerical matrix
- +: summation of polynomial matrix
- ==: equal operator for two polinomial matrices, result is a boolean matrix
- ==: equal operator for polinomail matrix and polinomail, result is a matrix
- ==: equal operator for polinomial and numerical matrices
- ==: equal operator for polinomial matrix and number, result is a matrix
- ==: equal operator for aby object and polinomial matrix
- !=: not equal operator
- !=: not equal operator
- %\*%: matrix multiplicatoin of polynomial matrices

- %\*%: matrix multiplicatoin of polynomial and numerical matrices
- %\*%: matrix multiplicatoin of numerical and polynomial matrices
- \*: scalar multiplication with number
- \*: scalar multiplication with polynomial
- \*: scalar multiplication of polynomial mattrices elementwise
- \*: scalar multiplication
- -: substractioin
- -: substractioin
- -: substractioin

### **Slots**

coef A matrix of coefficients which are joined into one matrix from lower degree to higher ncol Actual number of columns in the polynomial matrix

### **Examples**

```
# create a new polynomial matrix by parsing strings
pm <- parse.polyMatrix(</pre>
    "x; 1 + x^2; 3 x - x^2",
    "1; 1 + x^3; - x + x^3"
)
# get coefficient matrix for degree 0
pm[[0]]
     [,1] [,2] [,3]
##
## [1,] 0 1 0
## [2] 1 1 0
# get coefficient matrix for degree 1
pm[[1]]
      [,1] [,2] [,3]
## [1,] 1 0 3
## [2]
          0 0 -1
# dimensions
nrow(pm) ## 2
ncol(pm) ## 3
dim(pm) ## [1] 2 3
# round
round(parse.polyMatrix(
  " 1.0001 - x,
                          1 - x^2, 1 + 2.0003 \times x + x^2
 "0.0001 + x - x^2, 1 + x + 0.0001 x^2, 1 - 2*x + x^2"
```

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```
))
                                                      [,1] [,2] [,3]
1 - x 1 - x^2 1 + 2x + x^2
## [1,]
## [2,] x - x^2
                                                                                                      1 + x \quad 1 - 2x + x^2
# print out a polynomial matrix
show(parse.polyMatrix(
                                   1.0001 - x, 1 - x^2, 1 + 2.0000

1 + x - x^2. 1 + x, 1 - 2*x + x^2, 1 + x, 1 - x^2, 1 + x, 1 - x^2, 1 + x^
                                                                                                                                      1 - x^2, 1 + 2.0003 \times x + x^2
         "0.0001 + x - x^2,
                                                 12.3 x^3, 2 + 3.5 x + x^4, -0.7 + 1.6e-3 x^3"
))
                                           ##
## [1,]
## [2,] 1e-04 + x - x^2
## [3,] 12.3x^3 2 + 3.5x + x^4
```

polyMatrix.apply

Apply for polynomial matrix

### **Description**

Apply function to each element of matrix

### Usage

```
polyMatrix.apply(x, f)
```

# Arguments

x an polynomial matrix

f an function with only one argument

t,polyMatrix-method

Polynomial matrix transpose

# **Description**

Given a polyMatrix, t returns the transpose of x

### Usage

```
## S4 method for signature 'polyMatrix' t(x)
```

tr 25

# **Arguments**

x a polyMatrix

#### See Also

base::t() for numerical matrix tranpose

# **Examples**

tr

Trace of a 'matrix' or 'polyMatrix' class matrix

# Description

Trace of a matrix is the sum of the diagonal elements of the given matrix.

### Usage

tr(x)

### **Arguments**

Х

an matrix or a polynomial matrix

# **Details**

If the given matrix is a polynomial matrix, the result will be a polynomial.

### Value

Returns the trace of the given matrix as a number or a polynomial.

# **Examples**

```
# numerical matrices
m <- matrix(1:12, 3, 4)
## [,1] [,2] [,3] [,4]
## [1,] 1 4 7 10
## [2,] 2 5 8 11
## [3,] 3 6 9 12
tr(m) ## 15</pre>
```

26 triang\_Interpolation

triang\_Interpolation Triangularization of a polynomial matrix by interpolation method

### **Description**

The parameters point\_vector, round\_digits can significantly affect the result.

### Usage

```
triang_Interpolation(
  pm,
  point_vector,
  round_digits = 5,
  eps = .Machine$double.eps^0.5
)
```

# **Arguments**

```
pm source polynimial matrix
point_vector vector of interpolation points
round_digits we will try to round result on each step
eps calculation zero errors
```

### **Details**

Default value of 'eps" usually is enought to determintate real zeros.

In a polynomial matrix the head elements are the first non-zero polynomials of columns. The sequence of row indices of this head elements form the shape of the polynomial matrix. A polynomial matrix is in left-lower triangular form, if this sequence is monoton increasing.

This method offers a solution of the triangulrization by the Interpolation method, described in the article of Labhalla-Lombardi-Marlin (1996).

### Value

Tranfortmaiton matrix

triang\_Sylvester 27

triang_Sylvester Triangularization of a polynomial matrix by Sylvester method	triang_Sylvester	Triangularization of a polynomial matrix by Sylvester method
---	------------------	--

### **Description**

The function triang\_Sylvester triangularize the given polynomial matrix.

### Usage

```
triang_Sylvester(pm, u, eps = ZERO_EPS)
```

# **Arguments**

pm	an polynomial	matrix to	triangularize
la	F J		

u the minimal degree of the triangularizator multiplicator

eps threshold of non zero coefficients

#### **Details**

The u parameter is a necessary supplementary input without default value. This parameter give the minimal degree of the searched triangulizator to solve the problem.

In a polynomial matrix the head elements are the first non-zero polynomials of columns. The sequence of row indices of this head elements form the *shape* of the polynomial matrix. A polynomial matrix is in left-lower triangular form, if this sequence is monoton increasing.

This method search a solution of the triangulrization by the method of Sylvester matrix, descripted in the article Labhalla-Lombardi-Marlin (1996).

#### Value

T - the left-lower triangularized version of the given polynomial matrix U - the right multiplicator to triangularize the given polynomial matrix

#### References

Salah Labhalla, Henri Lombardi, Roger Marlin: Algorithm de calcule de la reduction de Hermite d'une matrice a coefficients polynomiaux, Theoretical Computer Science 161 (1996) pp 69-92

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zero.round

Rounds object to zero if it's too small

### **Description**

Rounds object to zero if it's too small

### Usage

```
zero.round(x, eps = ZERO_EPS)
## S4 method for signature 'polynomial'
zero.round(x, eps = ZERO_EPS)
## S4 method for signature 'polyMatrix'
zero.round(x, eps = ZERO_EPS)
```

# Arguments

x an R object

eps Minimal numerical value which will not treat as zero

### **Details**

```
By befault eps:

ZERO_EPS

## [1] 1e-05
```

# Methods (by class)

- polynomial: rounding of a polynomial means rounding of each coefficient
- polyMatrix: rounding of a polynomial matrix

### See Also

```
is.zero()
```

# **Examples**

```
# numerical
zero.round(1) ## 1
zero.round(0) ## 0
zero.round(0.1, eps=0.5) ## 0
zero.round(c(1, 0, .01, 1e-10)) ## 1.00 0.00 0.01 0.00
```

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```
# polynomials
zero.round(parse.polynomial("0.1 + x + 1e-7 x^2")) ## 0.1 + x
zero.round(parse.polynomial("0.1 + x + 1e-7 x^2"), eps=0.5) ## x
# polynomial matrix
zero.round(parse.polyMatrix(
 "1 + 0.1 x, 10 + x + 3e-8 x^2, 1e-8",
 "0.1 + x^2, .1 + 1e-8 x^4, 1e-8 x^5"
))
##
              [,1]
                       [,2] [,3]
## [1,]
          1 + 0.1x
                     10 + x
         0.1 + x^2
                        0.1
## [2,]
zero.round(parse.polyMatrix(
  "1 + 0.1 x, 10 + x + 3e-8 x^2, 1e-8",
  "0.1 + x^2, .1 + 1e-8 x^4, 1e-8 x^5"
), eps=0.5)
##
         [,1]
                  [,2] [,3]
## [1,]
          1
               10 + x
## [2,]
        x^2
                            0
```

zero\_lead\_hyp\_rows

Get zero lead hyper rows of size sub\_nrow of matrix M

### Description

Get zero lead hyper rows of size sub\_nrow of matrix M

# Usage

```
zero_lead_hyp_rows(M, sub_nrow, esp = ZERO_EPS)
```

### **Arguments**

M Numerical matrix sub\_nrow Size of hyper row

esp Machine epsilon to determinate zeros

### Value

vector of idx of hyperrows, NaN for columns without zeros

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zero\_lead\_rows

Get zero lead rows of matrix M

# Description

Get zero lead rows of matrix M

# Usage

```
zero_lead_rows(M, eps = ZERO_EPS)
```

# Arguments

M Numerical matrix

eps Machine epsilon to determinate zeros

# Value

vector of idx (length is equal to column number), NULL in case of error

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